Summary of Steps in Graphical Data Analysis

Step 1: Graph the data! Plot a graph of the independent variable (x axis) vs. the dependent variable (y axis). Make sure you include all of the components that a scientific graph should have (i.e. descriptive title, labeled axes, units, scientific symbols for variables, appropriate scale, etc...). Draw a line (it may be a straight line or a

curve) of best fit that best approximates your data. For discussion purposes we will use this set of data.

a (units)	b (units)
0.8	1.3
2.4	2.2
10.6	4.6
22.9	6.8
26.0	7.2



Step 2: Examine the Shape of the Graph! For us there are 4 possible shapes:



Step 3: Determine the proportionality statement!

(The symbol α means "proportional to")

- a) Linear relationship: a is directly proportional to b. Written as $a \alpha b$
- b) Exponential relationship: a is directly proportional to b^2 or b^3 or b^n . Written as $a \alpha b^n$ where n > 1
- c) Inverse relationship: a is directly proportional to b^{-1} or b^{-2} or b^n . Written as $a \alpha b^n$ where $n \le -1$
- d) Root relationship: a is directly proportional to $b^{0.1}$ or $b^{0.5}$ or b^n . Written as $a \alpha b^n$ where 0 < n < 1

***** If you are dealing with a linear relationship then move on to step 6. Otherwise continue on...*****

Step 4: Based on the relationship determined in step 3 create a new table of values. For our example we have a rising curve (or exponential relationship). Therefore we know that the proportionality statement is

IB Physics

 $a \alpha b^n$ where n > 1, but we want to determine whether n is 1, 2, 3 or 53. So we will start with n = 2. Therefore our new table of values will include b².

a (units)	b (units)	b^2 (units ²)
0.8	1.3	1.7
2.4	2.2	4.8
10.6	4.6	21.2
22.9	6.8	46.2
26	7.2	51.8

Step 5: Graph the New Data. In our example we would graph a vs. b^2 . If we find that the new graph of a vs. b^2 is a straight line going through the origin then we can conclude that the correct proportionality statement is $a \alpha b^2$, or that n = 2! We can move on to step 6.

<u>However</u>, if the new graph is still a curve or it does not go through the origin then we must try n = 3. And if that doesn't work we need to try n = 4. And so on until we get the correct proportionality.



Step 6: Transform the proportionality statement into an equation. Suppose you conclude that $a \alpha b^2$, then the corresponding equation would be $a = kb^2$, where k is a constant number (e.g. $a = 2.5b^2$ or $a = 0.7b^2$, etc...). How do we determine the value of k? It is equal to the slope of the straight line graph from step 5! In our example from above the slope of the a vs. b² graph is 0.5. Therefore we can conclude that the relationship between a and b is $a = 0.5b^2$.